

---

## Summary and Conclusion

The thesis is to investigate a new form of generalized closed sets called  $\psi^*$ - $\alpha$ -closed sets in topological and bitopological spaces.

The preliminary definitions and notations used in the thesis are presented in chapter 1.

In chapter 2,  $\psi^*$ - $\alpha$ -closed sets and  $\psi^*$ - $\alpha$ -open sets are introduced. Their properties and characterizations are studied. It is observed that  $\psi^*$ - $\alpha$ -closed sets form a topology and the closure operator defined for  $\psi^*$ - $\alpha$ -closed sets satisfies Kuratowski closure axioms. As an application of  $\psi^*$ - $\alpha$ -closed sets new spaces namely,  ${}_{\psi^*\alpha}T_c$ -space,  ${}_{\psi^*\alpha}T_\alpha$ -space,  ${}_{g\alpha}T_{\psi^*\alpha}$ -space,  ${}_{\alpha g}T_{\psi^*\alpha}$ -space and  ${}_{\psi g}T_{\psi^*\alpha}$ -space are defined and their interrelations are obtained.

The concepts of  $\psi^*$ - $\alpha$ -continuity, quasi  $\psi^*$ - $\alpha$ -continuity, perfectly  $\psi^*$ - $\alpha$ -continuity, totally  $\psi^*$ - $\alpha$ -continuity, strongly  $\psi^*$ - $\alpha$ -continuity and contra  $\psi^*$ - $\alpha$ -continuity are introduced in chapter 3. Properties, characterizations and interrelations between these maps are obtained.

Chapter 4 deals with  $\psi^*$ - $\alpha$ -irresolute maps and contra  $\psi^*$ - $\alpha$ -irresolute maps. The association of these maps with other existing irresolute maps are analyzed.

$\psi^*$ - $\alpha$ -closed maps,  $\psi^*$ - $\alpha$ -open maps, quasi  $\psi^*$ - $\alpha$ -closed maps, quasi  $\psi^*$ - $\alpha$ -open maps,  $\psi^*$ - $\alpha$ -homeomorphisms and  $\psi^*$ - $\alpha$ -quotient maps are introduced and their related properties are analyzed in chapter 5. Also the concepts  $\psi^*$ - $\alpha$ -compact spaces and  $\psi^*$ - $\alpha$ -connected spaces are determined and the standard results are derived.

In chapter 6,  $(i, j)$ - $\psi^*$ - $\alpha$ -closed sets and  $(i, j)$ - $\psi^*$ - $\alpha$ -open sets are defined in bitopological spaces. Properties and characterizations are analyzed.  $(i, j)$ - ${}_{\psi^*\alpha}T_c$ -space,  $(i, j)$ - ${}_{\psi^*\alpha}T_\alpha$ -space,  $(i, j)$ - ${}_{g\alpha}T_{\psi^*\alpha}$ -space and  $(i, j)$ - ${}_{\alpha g}T_{\psi^*\alpha}$ -space are defined and their interrelations among them are discussed.

In chapter 7,  $(i, j)$ - $\psi^*$ - $\alpha$ - $\sigma_k$ -continuous maps quasi  $(i, j)$ - $\psi^*$ - $\alpha$ -continuous maps, perfectly  $(i, j)$ - $\psi^*$ - $\alpha$ -continuous maps, totally  $(i, j)$ - $\psi^*$ - $\alpha$ - $\sigma_k$ -continuous maps, strongly

$(i, j)$ - $\psi^*$   $\alpha$ - $\sigma_k$ -continuous maps, contra  $(i, j)$ - $\psi^*$   $\alpha$ - $\sigma_k$ -continuous maps,  $(i, j)$ - $\psi^*$   $\alpha$ -irresolute maps and contra  $(i, j)$ - $\psi^*$   $\alpha$ -irresolute maps are introduced in bitopological spaces and their properties and interrelations are analyzed.

$(i, j)$ - $\psi^*$   $\alpha$ -closed and open maps, quasi  $(i, j)$ - $\psi^*$   $\alpha$ -closed and open maps and  $(i, j)$ - $\psi^*$   $\alpha$ -homeomorphisms are defined and their properties and characterizations are discussed in the final chapter.

### **The Recommendations for Future Study**

1. Weaker and stronger forms of  $\psi^*$ -closed sets may be defined and studied in topological spaces.
2. The concepts of  $\psi^*$ -closed sets may be extended to ideal and digital topological spaces.
3. Fuzzy  $\psi^*$ -closed sets may be defined and analyzed in fuzzy topological spaces.
4.  $\psi^*$ -locally closed sets may be defined and studied in topological and bitopological spaces.
5.  $\psi^*$ -closed sets may be defined and examined in supra topological spaces.